# Convex optimisation with applications to image processing

Part III, Michaelmas 2013

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Cambridge Image Analysis





#### Layout

#### Course format

- graduate level Part III, CCA, ...
- M/W/F 12-1pm, MR14
- 24 lectures
- 3-4 example sheets
- examinable (May/June 2014)
- CIA courses this year:
  - T. Valkonen Measure and Image, 11-12, MR14
  - C. Schönlieb Variational and PDE Methods, Lent



#### Image Processing







#### Goal:

# Extract "useful" information from the data that we have...

...by using what we know about the problem.



### The problem



original



noisy input



output?



# Denoising





# Denoising L2-TV





### Denoising L1-TV





# Inpainting







# Inpainting





#### Segmentation





#### **Course outline**

- 1. Convex Analysis
  - existence
  - subdifferentials, optimality, certificatess
  - conjugacy, duality
- 2. Solvers
  - first-order
  - interior-point
  - min-cut/max-flow
- 3. Applications
  - convex models, TV, SVM
  - combinatorial problems, relaxation, segmentation
  - convex approximations, lifting
  - sparsity, compressed sensing



#### Literature

- Boyd/Vandenberghe: Convex Optimization
- Rockafellar/Wets: Variational Analysis
- Ben-Tal/Nemirovski: Lectures on Modern Convex Optimization
- Paragios/Chen/Faugeras: Handbook of Mathematical Models in Computer Vision



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